Coupling of a simultaneous heat and water model with a distributed hydrological model and evaluation of the combined model in a cold region watershed

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Abstract:

Snow and frozen soil prevail in cold regions worldwide, and the integration of these processes is crucial in hydrological models. In this study, a combined model was developed by fully coupling a simultaneous heat and water model with a geomorphologically based distributed hydrological model. The combined model simulates vertical and lateral water transfer as well as vertical heat fluxes and is capable of representing the effects of frozen soil and snowmelt on hydrological processes in cold regions. This model was evaluated by using in situ observations in the Binggou watershed, an experimental watershed for cold region hydrology of the Watershed Allied Telemetry Experimental Research Project. Results showed that the model was able to predict soil freezing and thawing, unfrozen soil water content, and snow depth reasonably well. The simulated hydrograph was in good agreement with the in situ observation. The Nash–Sutcliffe coefficient of daily discharge was 0.744 for the entire simulation period, 0.472 from April to June, and 0.711 from June to November. This model can improve our understanding of hydrological processes in cold regions and assess the impacts of global warming on hydrological cycles and water resources. Copyright © 2012 John Wiley & Sons, Ltd.

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INTRODUCTION

In winter, frozen soil occupies 55–60% of the land surface of the Northern Hemisphere (Zhang et al., 1999; Zhang et al., 2003a) and 72% of that in China (Li et al., 2008). Besides having a significant effect on soil heat and water fluxes, such conditions play an important role in hydrological and ecological processes in cold environments. The water phase transition in freezing/thawing cycles significantly alters soil water potential, which influences water evaporation and redistribution in the soil (Konrad and Duquennoi, 1993; Stahli et al., 1999; Zhang et al., 2003b). The ice in frozen soil modulates hydraulic properties such as infiltration capacity and hydraulic conductivity and, in turn, influences soil water transfer (Lundin, 1990; Stahli et al., 1996; Stahli et al., 1999; Koren, 2006). The underlying impermeable frozen soil generally prevents rainfall and snowmelt from infiltrating into deep soil, which may influence runoff generation and groundwater recharge (Cherkauer and Lettenmaier, 1999; Nyberg et al., 2001; Slater et al., 2001; Bayard and Stahli, 2005; Bayard et al., 2005; Quinton and Carey, 2008; Woo et al., 2008). The total water content conserved in frozen soil is an important controlling factor of runoff generation in the thawing period (Stahli et al., 1999; Stahli et al., 2001; Wright et al., 2008). Runoff generation on hillslopes in cold regions is heavily influenced by the thawing depth of frozen soil, and its mechanisms differ from those in temperate regions. Both lateral and vertical soil water fluxes in cold regions are strongly dependent on soil freezing or thawing depths (Hayashi et al., 2007; Quinton and Carey, 2008). Therefore, detailed descriptions of frozen soil in hydrological models are indispensable for runoff prediction in cold regions (Takata, 2002; Hall et al., 2003; Luo et al., 2003). Models excluding frozen soil modules tend to underestimate snowmelt runoff and accumulated discharge (Stahli et al., 2001; Pohl et al., 2005). In the Northern Hemisphere, many rivers originate from highlands and mountainous regions where the soil is exposed to freezing temperatures. In the context of global warming, permafrost tends to degrade, and the penetration depth of seasonal frozen soil changes. Consequently, water resource availability and annual distribution are affected. Therefore, hydrological models that consider frozen soil are necessary for integrated water resource management.

Numerous frozen soil parameterisation schemes have been developed and tested (Harlan, 1973; Jansson and Haldin, 1979; Flerchinger and Saxton, 1989; Stahli et al., 1996;
Koren et al., 1999; Jansson and Moon, 2001; Woo et al., 2004; Koren, 2006; Li et al., 2009a; Li et al., 2010). Several have been incorporated into land surface models, such as the simple biosphere model version 2 (SiB2), the community/common land model, and the variable infiltration capacity (VIC) model (Cherkauer and Lettenmaier, 1999; Slater et al., 2001; Cherkauer and Lettenmaier, 2003; Li and Koike, 2003; Niu and Yang, 2006; Yi et al., 2006). In addition, frozen soil processes have been considered in distributed hydrological models such as the water and energy budget-based distributed hydrological model (WEB-DHM) (Wang et al., 2010), the GEOtop model (Rigon et al., 2006), the arctic hydrological and thermal process model (Zhang et al., 2000), the cold region hydrological model (Pomeroy et al., 2007), the distributed water heat coupled model (Chen et al., 2008), and others (Stahli et al., 1996; Stahli et al., 2001; Rawlins et al., 2003; Yamazaki et al., 2006). However, with the exception of VIC and GEOtop, most frozen soil schemes in hydrological models are simplified and empirical. Although some empirical schemes are capable of estimating the depth of soil freezing and thawing, they rarely simulate soil temperature and ice content or their influences on heat and water fluxes. Moreover, these schemes usually involve empirical parameters or formulae that must be calibrated for specific regions that vary with time (Stahli et al., 1999). VIC is designed for large scales from continental river basins to the entire globe, with spatial resolutions ranging from 1/8° to 2° (Liang et al., 1994; Cherkauer and Lettenmaier, 1999). On the contrary, GEOtop, which features three-dimensional soil water flux and one-dimensional energy balance, is designed for simulation in small watersheds with high spatial resolution (http://www.geotop.org/cgi-bin/moin.cgi). When applied to a large basin, the computational cost increases significantly. The efficient framework of WEB-DHM makes it practical for large basins. However, its frozen soil parameterisation is simple and empirical. Distributed hydrological models with physically based frozen soil modules remain in research.

The focus of this study is to couple a one-dimensional simultaneous heat and water model (SHAW) (Flerchinger and Saxton, 1989) with a geomorphologically based distributed hydrological model (GBHM) (Yang, 1998). The coupled model, SHAWDHM, addresses vertical heat and water fluxes in the soil vegetation atmosphere transfer (SVAT) system and lateral water flow on hillslopes. With this model, the impacts of vegetation, residue, topography, snow, and atmospheric conditions on soil freezing/thawing, and their influences on hydrological processes in cold regions can be fully considered. The coupled model was evaluated in the Binggou watershed, a small experimental watershed used for cold region hydrology studies in the Watershed Allied Telemetry Experimental Research (WATER) Project (Li et al., 2009b). This paper includes a review of relevant models and a description of the coupled model development in section 2. Background information of the study area and datasets are presented in section 3, and the results and conclusions are presented in sections 4 and 5, respectively.

Review of relevant models

The GBHM, originally developed (Yang, 1998; Yang et al., 2002) and further modified into grid-based style by Yang et al. (2004), employed hillslope as the basic hydrologic response unit. A sub-grid parameterisation method was used to consolidate the topographic information of a model grid into hillslopes on the basis of finer digital elevation model (DEM), which increases model efficiency when used in large watersheds. Essentially, the structure of hillslopes connected by a river network embodied in the model physically represents the spatial patterns of hydrological processes in a watershed. Wang et al. (2009a, b) coupled the GBHM with the three-layered Sib2. This coupled model, WEB-DHM, assimilated advantages from the physically based land surface model and improved the prediction of water and energy fluxes on a hillslope and stream discharge (Wang et al., 2009b; Jaranilla-Sanchez et al., 2011). Subsequently, the WEB-DHM was further improved by incorporating an empirical frozen soil module (Wang et al., 2010).

On the other hand, the SHAW model was designed to simulate soil freezing and thawing cycles. With more than 20 years in development, this model fully addresses the hydrological and thermal processes in a one-dimensional vertical profile extending either from the top of canopy, snow, or residue or from the soil surface to a specified soil depth (Flerchinger and Saxton, 1989). SHAW has an excellent record in simulating heat and water fluxes in the SVAT system in cold regions. The physical processes are governed by a set of partial differential equations that are solved simultaneously by the finite difference method. A discrete layered system was established to describe liquid, vapour, heat, and solute fluxes. This model can estimate soil freezing or thawing depth, temperatures, soil water and ice content, and solute concentration, as well as snow accumulation and ablation. Therefore, the SHAW model was selected for coupling with a distributed hydrological model because of its excellent performance in describing snow and frozen soil processes in cold regions.

Model development

The SHAW and GBHM were fully coupled under the framework of the grid-based GBHM (Yang et al., 2004; Wang et al., 2009a). The structure and lateral hydrological processes of GBHM were retained as a hydrological sub-model, whereas its vertical processes such as canopy interception, snowmelt, infiltration, and soil water transfer were replaced by those of SHAW. The hydrological sub-model and SHAW shared the same layered system, which includes vertical discretisation and state variables such as soil water content, ice content, and hydraulic conductivity. The coupled model, SHAWDHM, describes frozen soil processes and its relationship with snowmelt, infiltration, evaporation, and runoff generation in a physically based method to simulate the hydrological processes in cold regions.
In this section, the SHAWDHM is described in detail, as illustrated in Figure 1. The method for catchment discretisation is introduced, and a watershed is discretised into spatially distributed model grids. The topography of these grids is assumed to comprise homogeneous hillslopes on which GBHM and SHAW are coupled. The model components and the coupling strategy are subsequently detailed.

**Catchment discretisation.** The catchment discretisation was inherited from the grid-based GBHM. As shown in Figure 1 a), a watershed was first divided into nine sub-basins based on the DEM by using the method proposed by Pfafstetter. Each sub-basin can also be divided into nine (Pfafstetter, 1989; Verdin and Verdin, 1999). This recursive subdivision procedure had a maximum level of three; that is, a watershed can be divided into a maximum of 729 sub-basins. In each sub-basin, a series of flow intervals can be identified according to the flow distance to its outlet. This sub-basin and flow interval structure simplified the river routing procedure. Flow intervals were further divided into several model grids. Thus, the entire watershed was tiled by spatially distributed model grids.

The topography in a model grid was assumed to be hillslopes located along channels, as shown in Figure 1 b). Provided that the total river network length in a model grid extracted from finer DEM is \( \sum L \), the topography in the model grid can be consolidated as a couple of geometrically symmetrical hillslopes of length \( l = A/2 \sum L \) along the river, where \( A \) is the grid area (m²). In these virtual hillslopes, the canopy, residue, snow, and soil were divided into multiple layers parallel to the slope. The vertical heat and water fluxes and lateral water flows such as overland flow, interflow, and baseflow were simulated in the layered system.

**Model components and model coupling.** The same layered system as that for hillslopes was adopted for SHAW and GBHM, and they were coupled by sharing the same set of variables such as liquid soil water content, ice content, and soil hydraulic properties. In each time step, vertical heat and water fluxes, lateral water flows, and river routing were simulated in a coupled way. The model components and coupling strategy are described in detail as follows.
Step 1. Vertical heat and water fluxes. The SHAW model was initially run on the hillslopes. One-dimensional vertical heat and water fluxes in the SVAT system were governed by coupled partial differential equations based on energy and mass conservation as follows (Clapp and Hornberger, 1978):

\[ C_i \frac{\partial T}{\partial t} - \rho_i L_f \frac{\partial h_i}{\partial t} = \frac{\partial}{\partial z} \left( k_i \frac{\partial T}{\partial z} \right) - \rho_i c_i \frac{\partial q_i}{\partial z} - L_e \left( \frac{\partial \theta_i}{\partial t} - \frac{\partial \rho_i}{\partial t} \right) + R_e \]

(1)

\[ \frac{\partial \theta_i}{\partial t} + \frac{\rho_i \partial h_i}{\partial t} = \frac{\partial}{\partial z} \left( K_i \left( \frac{\partial \psi}{\partial z} + 1 \right) \right) + \frac{1}{\rho_i} \frac{\partial q_v}{\partial z} + U \]

(2)

The relationships between the soil matric potential (\( \psi \)), liquid soil water content (\( \theta_i \)), hydraulic conductivity (\( K \)), and soil temperature (\( T \)) can be established by the following equations (Clapp and Hornberger, 1978; Fuchs et al., 1978):

\[ \psi = \psi_e \left( \frac{\theta_i}{\theta_{e}} \right)^{-b} \]

(3)

\[ K = K_s \left( \frac{\theta_i}{\theta_{s}} \right)^{2b+3} \]

(4)

\[ \psi = \frac{L_v}{g} \left( \frac{T}{T_K} \right) \]

(5)

where \( C_i \) is the volumetric heat capacity of soil (Jm\(^{-3}\)°C\(^{-1}\)); \( T \) is the soil temperature (°C); \( t \) is time (s); \( \rho_i \) is the density of ice (kg m\(^{-3}\)); and \( L_f \) is the latent heat of fusion (335,000 Jkg\(^{-1}\)); \( \theta_i \) is the volumetric ice content of soil; \( k_i \) is the thermal conductivity of soil (Wm\(^{-1}\)°C\(^{-1}\)); \( z \) is the vertical distance from the surface (m); \( c_i \) is the specific heat capacity (Jm\(^{-3}\)°C\(^{-1}\)); \( q_v \) is the liquid water flux (m s\(^{-1}\)); \( q_s \) is the vapour water flux (kgm\(^{-2}\)s\(^{-1}\)); \( L_v \) is the latent heat of vapourisation of water (Jkg\(^{-1}\)); \( \rho_v \) is the vapour density of water (kgm\(^{-3}\)); \( R_n \) is the net downward radiation flux incident on the soil surface (Wm\(^{-2}\)); \( \theta_l \) is the volumetric liquid water content of soil; \( K \) is the hydraulic conductivity of unsaturated soil (m s\(^{-1}\)); \( \psi \) is the soil water potential (m); \( U \) is a source/sink term for water flux (m\(^{3}\)m\(^{-3}\)s\(^{-1}\)); \( \psi_e \) is the air-entry potential of soil (m); \( K_s \) is the hydraulic conductivity of saturated soil (m s\(^{-1}\)); \( b \) is the soil pore size distribution parameter; \( g \) is the acceleration of gravity (9.81 m s\(^{-2}\)); and \( T_K \) is the absolute soil temperature (K).

The coupled partial differential equations were discretised into implicit finite difference form and were solved by using the Newton-Raphson iteration technique. As a result, vertical heat and water fluxes can be estimated in addition to state variables in the SVAT system, including temperature, liquid water content, water vapour density, ice content, snow depth, snowmelt, infiltration, surface runoff, and surface water ponding. Moreover, the hydraulic conductivities of each soil layer were updated, and a simple groundwater aquifer node was added below the soil layers. Interactions between the groundwater and unsaturated zone were simulated by using Darcy’s law.

Step 2. Overland flow. In step 1, the infiltration excess was calculated by using the Green–Ampt equation (Green and Ampt, 1911; Clapp and Hornberger, 2000), and surface water storage \( h \) (m) was maintained. Overland flow along the hillslope surface was governed by Manning’s steady sheet flow. After overland flow calculation, surface water storage was updated and used as the upper boundary condition of the vertical water transfer problem in the next time step:

\[ \frac{\partial h}{\partial t} + \frac{\partial q_s}{\partial t} = i \]

\[ q_s = \frac{1}{n} S_0^{1/2} h^{5/3} \]

(6)

where \( q_s \) is the overland flow per unit width (m\(^3\)s\(^{-1}\)m\(^{-1}\)); \( h \) is the water storage depth (m); \( t \) is time (s); \( l \) is the distance along the hill slope (m); \( i \) is the net input rate (m/s); \( S_0 \) is the hill slope gradient; and \( n \) is the Manning roughness parameter.

Step 3. Subsurface flow. The lateral subsurface flow in the unsaturated soil along hillslopes is driven by gravity forces when the liquid soil water content is higher than the field capacity:

\[ q_{sub} = \sum_{i=1}^{N} K_i \Delta z_i \sin \alpha \]

if \( \theta_{f_i} > \theta_{e} \)

(7)

\[ q_{sub} = \max(q_{sub}, \Delta z_i (\theta_{f_i} - \theta_{e})) \]

where \( q_{sub} \) is subsurface flow per unit width (m\(^3\)s\(^{-1}\)m\(^{-1}\)); \( N \) is the number of soil layers; \( i \) is the soil layer index; \( z \) is the slope; \( K_i \) is the hydraulic conductivity of i-th soil layer (m s\(^{-1}\)); \( \Delta z_i \) is the thickness of i-th soil layer (m); \( \theta_{e} \) is the volumetric liquid soil water content of i-th soil layer; and \( \theta_{f} \) is the volumetric field capacity of i-th soil layer.

Step 4. Baseflow. Interactions between groundwater and river were calculated by using Darcy’s law. Hydraulic conductivity was adjusted according to the frozen depth of the aquifer. When the freezing front was deeper than the maximum soil depth prescribed in the model, Stefan’s equation was employed to estimate the frozen depth of the aquifer by using the bottom layer temperature as the driving force:

\[ q_g = K_s \left( 1 - \frac{D_f}{D_g} \right) \frac{H_1 - H_2}{L/2} + \frac{h_1 + h_2}{2} \]

(8)

where \( q_g \) is the baseflow per unit width (m\(^3\)s\(^{-1}\)m\(^{-1}\)); \( K_s \) is the groundwater hydraulic conductivity (m s\(^{-1}\)); \( L \) is the slope length (m); \( D_f \) is the thickness of the aquifer (m); and \( D_g \) is the frozen depth of aquifer (m). \( h_1, h_3, H_1, \) and \( H_2 \) are shown in Figure 2.

Step 5. River routine. A virtual channel was allocated for each flow interval. The channels were connected consecutively from upstream to downstream in the sub-basin to form a virtual river. Linked virtual rivers of all sub-basins comprised the virtual river network.
which accumulated the overland flow, subsurface flow, and baseflow from all grids. The runoff from each model grid entered the corresponding virtual channel and was routed through the network by using the kinematic approximation of the Saint Venant equations (Yang, 1998; Yang et al., 2002; Yang et al., 2004):

$$\frac{\partial Q}{\partial x} + \frac{\partial A}{\partial t} = q = q_s + q_{sub} + q_g$$

(9)

$$Q = \frac{1}{n} \frac{S_0^{1/2}}{p^{3/2}} \cdot A^{5/3}$$

(10)

where $Q$ is the discharge at a given river section ($m^3s^{-1}$); $x$ is the distance along the longitudinal axis of the river (m); $A$ is the cross-sectional area ($m^2$); $q$ is the lateral flux in each flow interval, including overland flow, subsurface flow, and baseflow ($m^2s^{-1}$); $n$ is the Manning roughness; $p$ is the wetted perimeter (m), i.e. the length of a line in contact with the water; $t$ is time (s); and $S_0$ is the river bed slope.

Step 6. Return to Step 1 and repeat for next time interval.

MODEL EVALUATION

Study area

The coupled model was evaluated in the Binggou watershed (100°12’–100°18’E and 38°1’–38°4’N), which is an experimental watershed for cold region hydrology of the WATER Project (Li et al., 2009b). The watershed, located in the upper reaches of the Heihe River basin in northwest China, covers an area of 30.4 km² and is a high mountainous head watershed with elevations ranging from 3440 to 4400 m. The watershed is in a typical cold region where frozen soil is common. Observations from 1984 to 1991 indicate that the long-term average annual air temperature was approximately −2.5°C at an altitude of 3,450 m, and the minimum air temperature reached −30.8°C (Yang et al., 1993). Both permafrost and seasonal frozen soil exist in the watershed. Regions higher than 4000 m are dominated by permafrost, whereas seasonally frozen soil is distributed in areas below 4000 m. The mean annual precipitation is approximately 686 mm. Snowfall prevails from October to April, accounting for approximately 30% of the total precipitation.

Datasets

Meteorological data. In the WATER project, two stations were installed in the watershed: Dadongshu Snow Observation Station (DY, at 100°14’E, 38°01’N; 4,146.8 m) and Binggou Station (BG, at 100°13’E, 38°04’N; 3,449.4 m); see Figure 3. The DY station was equipped with an automatic weather station and an ultrasonic snow depth sensor (SR50). Continuous meteorological forcing data, soil temperature and moisture, snow depth, and other fluxes were obtained from 1 November 2007 to 21 November 2008 (Li and Wang, 2011). At one of the automatic weather stations at BG, only the meteorological forcing data (without precipitation) and soil temperature from 14 March 2008 to 31 December 2009 were collected owing to battery malfunction.

Meteorological data measured at DY were used to derive hourly spatially distributed forcing data. Hourly meteorological series were first aggregated from the 10-min logged raw data at DY. Because of the lack of data, the relative humidity, precipitation, wind speed, and downward shortwave radiation in the watershed were assumed as spatially uniform, and values were taken from the DY station. This assumption is reasonable since the watershed is relatively small. When overlap existed in observing time between BG and DY, i.e. from 14 March 2008 to 21 November 2008, air temperatures in the watershed were interpolated against elevations based on
measurements at both stations. Average hourly air temperature lapse rates of all days from March to November, as well as those in months with observations, were calculated and sketched (Figure 4). The former was used to interpolate air temperatures against elevations in December, January, and February on the basis of DY observations. Note that the snowfall measured by rainfall gauge was significantly underestimated in winter and spring. A more realistic snowfall series was derived from observed snow depths. When air temperature was below the freezing point and the increase in snow depth per hour was greater than 2 cm, equivalent water corresponding to the snow depth increase was converted to precipitation. The required snow density was calculated as an empirical function of air temperature in the following equation, where $T$ is the air temperature ($^\circ$C) (Schmidt and Gluns, 1991; Hedstrom and Pomeroy, 1998; Pomeroy et al., 1998). After the correction of snowfall in winter and spring, the total precipitation was 703 mm in the watershed.

\[ \rho_{\text{snowfall}} = 67.9 + 51.3e^{T/2.6} \]  

Vegetation and soil data. The dominant land cover type in the watershed is alpine meadow at altitudes of 3440–4000 m; the region above 4000 m is mainly alpine desert. The dynamic leaf area index (LAI) was obtained from 8-day composites (MOD15A2) of the Moderate Resolution Imaging Spectroradiometer that were interpolated into daily series. Because no dedicated soil surveys had been conducted in the region, the Harmonized World Soil Database (HWSD, http://www.iiasa.ac.at/Research/LUC/External-World-soil-database/HTML) was used to obtain the distributed soil properties. The soil map of China in the HWSD database was from the Second National Soil Survey of China (1995) conducted by the Institute of Soil Science of the Chinese Academy of Sciences (Shi et al., 2004). In the database, soil columns were divided into two layers: a top layer (0–30 cm) and a sub-layer (30–100 cm). Physical soil properties include fractions of sand, silt, and clay; organic content; and bulk density. With these properties, the soil pore size distribution index, air-entry potential, and other hydraulic parameters required by the model were derived by using the method proposed by Saxton (Saxton and Rawls, 2006).

Model setup and calibration

The model adopted a spatial resolution of 250 m. The average soil depth was assumed to be 1.2 m in the watershed. Soil columns were divided into 11 layers, each of which was represented by one central node at 0, 0.05, 0.10, 0.15, 0.20, 0.30, 0.40, 0.60, 0.80, 1.00, and
1.20 m below the soil surface. The lower Dirichlet boundary condition of soil temperature was estimated by using the method proposed by Hirota et al. (2002), which required the mean annual temperature of deep soil (MAT, at 120 cm). The spatially distributed MATs were interpolated against elevations on the basis of observations made at DY with a mean lapse rate, which was calculated from observations at DY and BG to be approximately $-7 \, \text{K km}^{-1}$. For the water transfer problem, a unit gradient of soil water potential was assumed as the lower boundary condition.

The model was run in hourly steps from 20 November 2007 to 20 November 2008. Only point scale calibration was conducted at DY to obtain the dry soil albedo, canopy albedo, and residue albedo, which were 0.3, 0.24, and 0.3, respectively. Other parameters were assigned as those following either field observations or recommended values in the SHAW user manual. Owing to data limitations, several parameters, including roughness length for overland flow, momentum, and heat turbulence, were assumed as spatially uniform. Wang et al. (2010) conducted relevant works in the watershed with WEB-DHM, in which the same hydrological sub-model (i.e. GBHM) was used. Therefore, values for relevant parameters calibrated by Wang et al. (2010) were used in this study. These parameters included flow interval width, river width, river depth, Manning’s coefficient, and riverbed slope. The initial distributed depth of groundwater table, snow depth, and soil water content were assigned according to the results of one-year spin-up period with forcing data from 20 November 2007 to 20 November 2008. The initial distributed soil temperatures were interpolated against elevations based on the soil temperature profile observed at DY on 20 November 2007.

RESULTS AND DISCUSSION

The root mean square error (RMSE) was used to quantitatively evaluate the model performance in simulating soil temperature and water content, and it was calculated as follows:

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (\tilde{y}_i - y_{oi})^2}$$

(12)

where $y_{oi}$ is the observed series; $\tilde{y}_i$ is the simulated series; and $N$ is the number of observations. The Nash–Sutcliffe coefficient (NSE) was used to assess the performance in predicting stream discharge:

$$NSE = 1 - \frac{\sum_{i=1}^{N} (Q_{si} - Q_{oi})^2}{\sum_{i=1}^{N} (Q_{oi} - Q_{mo})^2}$$

(13)

here $Q_{si}$ is the simulated discharge series; $Q_{oi}$ is the observed series; and $Q_{mo}$ is the mean of observed discharge. A high NSE indicates good model performance. An NSE value of 1 denotes a perfect match.

Snow pack and frozen soil evolutions

Figure 5 illustrates the spatial distribution of simulated snow depth and associated statistics. In general, snow began to accumulate in October or November in the watershed. At the beginning of accumulation, snow distribution was strongly related to topography because snowmelt was sensitive to air temperature. Higher regions with lower air temperatures enabled greater snow accumulation. In lower regions, higher or even positive
Air temperatures resulted in rapid snowmelt. The snow in most regions reached maximum depths in February or March. However, snow distributions in March and April differed from that in November. They depended more on the total cumulative precipitation than on air temperature during winter and spring, since the air temperatures in winter were far below the freezing point, which was not beneficial to snowmelt. In March, snow in the lower regions began to melt and extended gradually to higher areas with increased air temperatures in April and May (Yang et al., 1993). The snow cover usually disappeared in June in the watershed. However, significant snow accumulation of short duration occurred in some regions in early summer, which was confirmed by observation at DY (Figure 6).

The simulated and observed snow depths at DY from 21 November 2007 to 20 November 2008 are presented in Figure 6. Initially, the snow depth was in good agreement with the measurements when no significant snowfall occurred. However, from January onward, the simulated snow depth was occasionally underestimated. This may be attributed to the underestimated solid precipitation derived from the snow depth, as previously mentioned. Only an increase in snow depth greater than 2 cm per hour was identified as snowfall. Continuous light snowfall was ignored as noise when no significant snow depth increase per hour was observed. In addition, errors could be introduced by the empiric equation for snow density estimation because the equation was originally proposed for snowfall in forests. Regardless of the occasional discrepancies, however, the model yielded overall realistic snow depth prediction; RMSE was 0.033 m.

Figures 7 and 8 illustrate spatially distributed penetration depths of soil thawing and freezing fronts, respectively.
Soil thawing began from the lower regions in late April and early May and progressed to ridge areas with an increase in air temperature. The thawing fronts reached maximum depths in mid-September, and the seasonal frozen soil melted completely. In late September, the soil began to refreeze. According to the survey by Yang et al. (1993), permafrost was distributed above 4000 m in the watershed, as indicated by black lines in Figures 7 and 8. The simulated seasonal frozen soil region is represented by the dark brown region in the lower right-hand panel of Figure 7; the other region is permafrost. These results are clearly consistent with Yang’s survey. In addition, the observed soil thawing depths derived from the soil temperature profile and the simulated values at DY are compared in Figure 9. The frozen soil began to melt on 1 May. The melting was mainly constrained within the surface layer at approximately 0–25 cm. In June, the thawing front began to penetrate downward. In September, the thawing process ceased, and the soil began to refreeze from the surface downward. The simulated maximum thawing depth was slightly underestimated at DY. This discrepancy may be attributed to the substantial thicknesses of soil layers prescribed in the model, which can cause inaccuracies in soil temperature simulation. The lower boundary condition of temperature could be an additional explanation. The simulated soil temperature at the lower boundary layer at 120 cm was slightly underestimated, as shown in Figure 10.

Soil temperature

Simulated soil temperatures at DY were compared with in situ observations (Figure 10). From February to March, the simulated soil temperatures near the surface (at 5, 10, and 20 cm) were obviously higher than the observed values when air temperature increased; the temperatures of deep soil were not affected by these warming events. These results may be attributed to underestimated snow depth (Figure 6), which did not provide adequate insulation from the warm air. Therefore, the soil warmed noticeably faster than observed temperatures. From March onward, the discrepancy between the simulated and observed temperatures began to diminish as the simulated snow depth became more consistent with measurements. From 7 April 2008, the observed soil temperatures increased nearly to the freezing point and decreased soon afterward. Large cracks may exist in the soil column, which allow warmer melt water from the surface to percolate rapidly into deep soil, providing a warming source. The soil temperatures decreased after refreezing of the melt water. The model failed to reproduce the soil temperatures of the top layers from September to November 2008. As shown in the top panels of Figure 10, simulated temperatures remained
positive for a lengthy period while the surface soil began to refreeze.

Figure 11 presents a comparison of simulated and observed soil temperatures at BG. The soil temperatures in summer were slightly underestimated, which may be attributed to the heterogeneity of vegetation and soil parameters such as LAI and thermal conductivity. Overall, the combined model reliably predicted soil temperatures in the watershed.

Liquid soil water content

Observation of liquid soil water content at BG was erroneous owing to sensor malfunction; therefore, only observations at DY were used to evaluate the model. Figure 12 presents a comparison between the observed and simulated volumetric liquid soil water content at DY. The surface soil began to melt on 15 May. However, the melting
process was constrained to the first 15 cm below the surface; deeper soil remained frozen. Snowmelt from the surface was perched above the thawing front because of the impermeable underlying frozen soil. This explained the observed peak of liquid water content at 10 cm. However, the simulated peak value was lower because the corresponding simulated soil thawing depth was a little deeper (Figure 7). Perched water in the model was not as significant as the measurement. When frozen soil thawed downward, the perched water infiltrated rapidly, and the soil water content decreased. The model captured the pattern of liquid soil water content, although some discrepancy occurred between the simulated and observed values. This result is expected because the complexities of actual conditions cannot be fully modelled, particularly in mountainous areas with high heterogeneity in soil properties, vegetation structure, and topography.

Stream discharge

A stream flow gauge was installed at BG in 2008. The stream flow rate was measured hourly during the initial stage of hydrography to determine the timing of diurnal maximum and minimum. The flow rate was then measured at least three times daily. The average daily discharge was aggregated from measurement and was compared with simulated values during the period from 17 January 2008 to 20 November 2008, as shown in Figure 13. Figure 14 compares hourly simulated discharge with observed values.
Snow began to melt in March from the lower regions of the watershed. Because the melting extent was limited, the runoff was initially small. As the air temperature increased in April, the snowmelt extended rapidly toward upper slope regions (upper right-hand panel in Figure 5); meanwhile, only surface soil thawed in the watershed (Figure 7). The underlying frozen soil prohibited snowmelt from infiltrating downward. Therefore, the snowmelt runoff was greatly enhanced, and the peak discharge was even higher than that in summer (Yang et al., 1993). In addition, the snowmelt runoff showed high diurnal variation because the heat source for melting was higher in the daytime and lower at night.

As shown in Figures 13 and 14, the diurnal peak values of simulated discharge from April to May were higher than those observed, whereas the simulated daily discharge was in good agreement with the measurement. NSE of daily discharge from March to May was 0.472. The peak discharge in mid-August was underestimated. The discharge in fall and winter was generally smaller than observation. Although the watershed is small, precipitation varies in mountainous areas owing to orographic effects. Errors may be introduced when uniformly distributed precipitation is assumed, which may explain the underestimated discharge. In addition, continuous light snowfall was ignored as noise because the method used to derive precipitation from snow depth was based on a threshold of 2 cm. Another important factor is that the baseflow is complicated in the watershed. The method used in the model was not sufficient to depict the baseflow in such mountainous areas subject to both seasonal frozen soil and permafrost. Moreover, errors in soil temperature simulation could also lead to discharge underestimation in fall and winter. As shown in the top panels of Figure 10, measurements indicated that the surface soil at 5 and 10 cm began to refreeze in September, which would prohibit snowmelt and rainfall from infiltrating, thus enhancing the surface runoff. In contrast, the corresponding simulated soil temperatures remained positive for a lengthy period.

Overall, the simulated discharge agreed well with observations. NSE of the daily hydrograph was 0.744 in the entire simulation period and 0.711 from June to November. NSE of the hourly discharge was 0.711. Figure 15(a) presents a scatter plot of observed discharge versus corresponding simulated values; the
correlation coefficient was 0.849. Figure 15(b) presents cumulative curves of simulated and observed daily discharge. Inspection of the curves shows that the model performance was acceptable in spring and early summer. The model underestimated discharge in fall and winter. The total runoff was underestimated by approximately 13%.

Water balance

The total precipitation was approximately 703 mm in the watershed during the entire simulation period. The simulated evapotranspiration of 296 mm is slightly larger than the average annual value of 238 mm estimated by Yang et al. (1993), which was calculated according to a water balance analysis by using observations of steam runoff and precipitation from 1984 to 1991. According to the model, the runoff depth of the watershed was approximately 488.4 mm, and the water storages of soil, groundwater system, and snow cover were decreased by 34.5 mm, 38.8 mm (average soil water content decreased from 0.384 to 0.352), and 5.7 mm, respectively. In any time step, the surface runoff from all model grids was summed as the total surface runoff at the watershed outlet without consideration of river routing. The total subsurface flow and baseflow could be estimated in the same manner. The subsurface flow accounted for approximately 69.6% of the total runoff, while the surface flow and baseflow accounted for 14.1% and 16%, respectively. As shown in Figure 16, surface runoff mainly occurred in the snowmelt season with shallow underlying frozen soil. In other seasons with deep frozen soil, surface runoff rarely occurred, even in summer with extensive precipitation.

CONCLUSIONS

Snow and frozen soil prevail in cold regions worldwide, and their effects on hydrological processes and water resources remain research focuses in the context of global climate change. In this study, the SHAW and GBHM models were fully coupled, and the combined model assimilated advantages from both components. The model simultaneously simulated the vertical and lateral water transfer as well as the vertical heat fluxes on hillslopes and considered the effects of frozen soil and snowmelt on hydrological cycles on a watershed scale. In addition, the heat and water fluxes were described in a physically based manner and region-specific empirical parameters were eliminated; however, the model required additional spatially distributed inputs.

The model was evaluated in the Binggou watershed, a small mountainous watershed in a cold region, and the results were compared with in situ observations. The simulated soil temperature, liquid soil water content, and snow depth were highly consistent with field observations. Although no spatially distributed observations were available to evaluate simulated soil freezing, thawing, and snow depth in the watershed, their spatial temporal changes were reasonable and in compliance with facts. The permafrost region determined by the model was in good agreement with the survey reported by Yang et al. (1993). The model showed good performance in simulating soil freezing/thawing and snow accumulation/melting. Both frozen soil and snow played important roles in stream discharge. Because the simulated snowmelt and frost table were reasonable, the discharge prediction was accurate in spring and early summer. However, peak runoff in summer and discharge in fall and winter were underestimated. The cumulative simulated runoff was approximately 13% smaller than that measured. According to the model, surface runoff in the watershed mainly occurred in snowmelt season with shallow underlying frozen soil. These results prove that the coupling strategy is reasonable, and the combined model is practical for cold regions.

Frozen soil, snowmelt, groundwater, and other processes are correlated in cold regions. To assess the impacts of global warming on hydrological cycles and water resources in such environments, these components should be properly integrated. The absence or erroneous representation of one process in the modelling system would result in errors in other processes. In mountainous areas subject to both seasonal frozen soil and permafrost, the groundwater flow is complicated. However, the influences of frozen soil on groundwater flow were resolved in a simple and rough manner. Lateral groundwater interaction between the model grids was also ignored in the model. A more robust groundwater flow module should be incorporated to improve the baseflow prediction. In addition, uncertainties from inputs account for a large part of uncertainties in the simulation. To better understand the hydrological processes in cold regions, an integrated watershed observation system is critical (Li et al., 2009b), particularly in mountainous regions. Retrievals of distributed forcing data, state
variables of the land surface system, and relevant model parameters such as soil and vegetation together form the cornerstone of watershed scale model development, improvement, and verification.

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COUPLING FROZEN SOIL MODEL WITH A DISTRIBUTED HYDROLOGICAL MODEL